Homomorphic Hybrid Encryption Technique using IKC and IEC Algorithms

Aakanksha Pundir, Sumit Chaudhary

Abstract: Distributed computing is a plausible, practical, and affirmed conveyance stage for giving business or shopper IT administrations in abundance of the Internet. For the best Performance and most superb security of distributed computing, we proposed Homomorphic half and half encryption strategy. With the advancement of Cloud Computing, Computer Network and Communication Technology, an enormous gathering of information and data require to be traded by open correspondence systems. High adequacy and high security of information transmission turn out to be a great deal more essential. In this paper we proposed Homomorphic Encryption strategy, Identity based Key Cryptosystem (IKC) and Identity based Encryption Cryptosystem (IEC) are broadly utilized two calculations of topsy-turvy encryption innovation. Both are ideal and top protection homomorphism, mix of IEC and IKC recharged to half breed calculation, which are capable to secure cloud information since Homomorphic encryption permits direct scrambled correspondence in distributed computing. Here first we are producing key from IKC then these private and open keys took after by IEC with the end goal of encryption/decoding, later Homomorphic encryption is connected for a protected encoded correspondence of clients in distributed computing.

Keywords - Cloud, cryptosystem, distributed, homomorphic.

I. INTRODUCTION

The encryption calculation E (.) is Homomorphic if determined E(a) and E(b), one can discover E(a + b) without unscrambling a, b for some operation +. Here we are using IEC and IKC as follows:

A. Identity based Key Cryptosystem

For key era here in this paper we are utilizing Identity based Key cryptosystem (IKC), two or three cryptographic keys (open key and private key) has given to every client. The private key is kept mystery, even as people in general key might be by large and circulated and the private key is kept mystery. The beneficiary's open key is utilized for encoding the message and message can be unscrambled with the related private key. The keys are unified scientifically, yet the private key can't be gotten from the general population key. Recognizable proof of the client is most imperative so the private key can't be gotten from the general population key. Th

B. Identity based Encryption Cryptosystem

As encryption and unscrambling are speak strategies, there must be a numerical association between the encryption and decoding keys. Security out in the open key cryptosystems depends on this relationship being one that can't just be abused to expect the (private) unscrambling key from information of (people in general) encryption key: The essential scientific issue that would deliver the decoding key from the encryption key must be computationally infeasible to translate. In Identity based Encryption Cryptosystem (IEC), the hidden scientific relationship between the encryption and unscrambling keys depends upon the supposed discrete log issue.

Here we are utilizing keys from IKC and overhauling it with IEC.

Key generation:

Open key (n,g) and private key (λ,μ) taken by Key calculation and a few adjustments by Encryption for key era are taken after:

- Random numbers and cyclic gathering G taken by IKC.
- A figures z = gk1
- A distributes h, alongside all parts so (G, g,z,n)as her open key. Furthermore, holds (k1, λ,μ) as his private key.

Encryption:

A ready to encode his message m under his open key (G,g,z, n)

- B picks an irregular k2 from (A's characters), then computes c1=gyn.
- B computes the mutual mystery s=zk2.
- B maps his mystery message m onto a component m' of G.

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- B computes $c_2 = m'.s$
- B sends the ciphertext $(c_1, c_2) = (g^{k_2}, m'. z^{k_2}) = (g^{k_2}, m'. (g^{k_1} z^{k_2}))$ to A.

Decryption: Decoding done by ciphertext $(c_1, c_2)$ with his private key $x$.
- A calculates the mutual mystery $s = c_1^x$
- Then processes $m' = c_2 s^{-1}$ then changes over once again into the plaintext message $m$, where $s^{-1}$ is the reverse of $s$ in the gathering $G$.
- The decoding calculation creates the proposed message, subsequent to $c_2 s^{-1} = m' z^{k_2} (g^{-k_1 k_2}) = m' g^{k_1 k_2} g^{-k_1 k_2} = m'$.

![Diagram](attachment:diagram.png)

**Figure 1**: Pseudonymous flow chart for key generation by IKC + IEC and message encryption/decryption by Encryption cryptosystem

## II. RELATED WORK

X.Li et al. [1] in his paper has examined the security of Encryption computerized signature calculation under the four assault plan. He endeavored to build the security of Encryption calculation by adding an irregular number to the first one and along these lines making trouble in interpreting key. Nentawe Y. et al. [2] in this paper creator has introduced information encryption and decoding in a system domain that was effectively executed. S. Subasree, N. K. Sakthivel et al. [3] this convention gives three cryptographic primitives, for example, trustworthiness, privacy and validation. These three primitives can be accomplished with the assistance of Elliptic Curve Cryptography, Dual-RSA calculation and Message Digest MD5. That is it utilizes Elliptic Curve Cryptography for encryption, Dual-RSA calculation for verification and MD-5 for honesty. P. Gutmann et al. [4] this book gives a complete configuration to a compact, adaptable high-security cryptographic design, with specific accentuation on joining thorough security models and practices. Suyash Verma et al. [5] this paper creators proposed another calculation for assessments, results computation utilizing diverse plaintexts as a part of the same key (DPSK) mode. As the premise of the assessing procedure, the plaintext and the relating key are both created by haphazardly. Ravindra Kumar Chahar et.al [6] another security convention for on-line exchange can be composed utilizing mix of both symmetric and uneven cryptographic methods.
This convention gives three cryptographic primitives - honesty, classification and validation. It utilizes elliptic bend cryptography for encryption, RSA calculation for verification and MD-5 for respectability. Rather than ECC symmetric figure (AES-Rijndael) can be utilized to encode, open key cryptography (RSA) to verify and MD-5 to check for respectability.

Guilin Wang et al. [7] in this paper the creator have proposed another computerized contract marking convention in view of RSA advanced mark plan.

WANG Shaobin et al. [8] in this paper, creators portrays a strategy for developing proficient reasonable trade conventions in view of enhanced DSA marks the issue of reasonable trade is of the significant dangers in the field of secure electronic exchanges. In this paper the creators have displayed a multi signature plan taking into account DSA.

Afolabi, A.O et al. [9] this study proffered answer for some recognized information instability issues in programming improvement by the utilization of Web-based learning framework as a proving ground and advancement of a half breed crypto-biometric security framework. Arjen K. Lenstra et al. [10] we performed an once-over to verify everything is ok of open keys gathered on the web. Our principle objective was to test the legitimacy of the presumption that diverse irregular decisions are made every time keys are produced. We found that most by far of open keys act as expected.

Arvind Negi et al. [11] this paper introduced a novel component of creating computerized signature utilizing RSA calculation. The security of the framework is moderately upgraded utilizing this methodology. This system includes the utilization of various open key examples which thusly gave numerous open key and private key.

III. PROPOSED WORK

Here we are chipping away at Hybrid Homomorphic Encryption method. In this paper our fundamental origination was to scramble the information before to sending them to the Cloud source.

The user wants to allow the private key to the server to unscramble the information earlier to perform the figurings required, which may concern the mystery of information put away in the Cloud.

In this strategy first we are creating keys from proposed IKC and these private and open keys are trailed by proposed IEC with the end goal of encryption and unscrambling, open and private keys again redesigned by IEC for more security and later we are applying mix of Homomorphic Encryption procedure (HIKC+HIEC) for cloud source.

The critical reason of Homomorphic Encryption strategy can perform operations of scrambled information without decoding them.

A. Basic Flowchart for proposed methodology

![Figure 3: Basic Flowchart for proposed methodology](image)

**B. Main Algorithm for proposed methodology**

1. **Key Generation**
   - A Choose two large prime numbers a and b randomly from (Identity of B’s) and independently of each other such that gcd(ab,(a-1)(b-1))= 1
   - A Compute RSA modulus n = ab and Carmichael’s function \( \lambda = \text{lcm}(a-1, b-1) \) it can be computed using \( \lambda = \frac{(a-1)(b-1)}{\gcd(a-1,b-1)} \)
   - A Select generator g randomly from G, where G is a cyclic group of identities of 2nd person gcd \((g\lambda \mod n^2 - 1)/n, n) = 1, n is number in cyclic group.
   - There are \( \phi(n) \) * \( \phi(n) \) number of valid generators, therefore the probability of choosing them out of \( n\phi(n) \) elements of G is relatively high for big n.

![Figure 2: Flowchart for Hybrid Homomorphic Encryption (HHE) in Cloud Computing](image)
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- Calculate the following modular multiplicative inverse
  \[ \mu = ((g^4 \mod n^2))^{-1} \mod n \]

  The public (encryption) key is \((n, g)\).

  The private (decryption) key is \((\lambda, \mu)\).

Step 2. Key Updating

- Compute \( z = g^{k_1} \)
- Public key \((n, g)\) and private key \((\lambda, \mu)\) taken by Key algorithm and some modifications by Encryption for key generation are follows:
- Random numbers and cyclic group \(G\) taken by Key
- \(A\) computes \( z = g^{k_1} \)
- \(A\) publishes \( h\), along with all components so \((G, g, z, n)\) as her public key. And holds \((k_1, \lambda, \mu)\)
- The public (encryption) key is \((G, n, z, g)\).

Step 3. Encryption

A able to encrypt his message \(m\) under his public key \((G, g, z, n)\)
- \(B\) chooses a random \( y \) from \((A’s\ identities)\), then calculates \(c_1 = g^{k_1} \).
- \(B\) calculates the shared secret \(s = z^{k_2}\).
- \(B\) maps his secret message \(m\) onto an element \(m’\) of \(G\).
- \(B\) calculates \(c_2 = ms\).
- \(B\) sends the ciphertext \((c_1, c_2)\) to \(A\).

Step 4. Decryption:

Decryption done by ciphertext \((c_1, c_2)\) with his private key \(x\),
- \(A\) calculates the shared secret \(s = c_1^{k_1}\).
- Then computes \(m’ = c_2^{s^{-1}}\) then converts back into the plaintext message \(m\), where \(s^{-1}\) is the inverse of \(s\) in the group \(G\).
- The decryption algorithm produces the intended message, since \(c_2^{s^{-1}} = m’ h^{k_2} (g^{k_1 k_2} z^{k_2}) = m’ g^{k_1 k_2} = m’\).

Step 5. Homomorphic Property

- The encryption of a message is,
  \[ E(m) = (g^r, m \cdot h^r) \text{ for some } r \in \{0, \ldots, q - 1\} \]
- The homomorphic property for \(m_1\) and \(m_2\) in IEC is:
  \[ E(m_1) \cdot E(m_2) = (g^{r_1}, m_1 \cdot h^{r_1}) \cdot (g^{r_2}, m_2 \cdot h^{r_2}) = (g^{r_1 + r_2}, (m_1 m_2) h^{r_1 + r_2}) = E(m_1, m_2) \ldots \]
- The encryption of a message is
  \[ E(x) = g^x \mod m^2 \text{ for some } r \in \{0, \ldots, m - 1\} \]
- The homomorphic property for IKC is:
  \[ E(m_1), E(m_2) = (g^{q x_1}, m_1) \cdot (g^{q x_2}, m_2) \mod m^2 = (x_1 + x_2 \mod m^2) \cdot m^2 \]
- From equations 1 & 2 -
  \[ E(m_1), E(m_2) = E(m_1, m_2) \ldots E(x_1), E(x_2) = E(x_1 + x_2 \mod m^2) \]
- Here we are changing values of \(x\) and \(m\), for concatenation of both encryption techniques. Now, \(m_1 = x_1 \mod m_2 = x_2\). So, \(E(m_1), E(m_2) = E(x_1), E(x_2) \)

Step 2. Encryption

- \(B\) chooses a random number \(k_2\) from \((A’s\ identities)\), then calculates \(c_2 = g^{k_2}\).
- If \(k_2 = 3\), \(S = 4096\).
- \(B\) calculates the shared secret \(s = z^{k_2} = 16^3 = 4096\).
- \(S = 4096\).
- \(B\) maps his secret message \(m\) onto an element \(m’\) of \(G\), if \(m’ = 2\).
- Then \(c_2 = m^2 \cdot s = 16 \cdot 4096 = 65536\).

C. Mathematical Proof as Implementation

Key Generation

- \(B\) chooses two prime numbers from \(B’s\ identity, suppose \(B\) having an identity which vary from \((0\ to\ 30)\). And same \(A’s\ identities vary from \((0\ to\ 20)\).
- \(a = 3, b = 11\)
- \(gcd(\ (a-1)\ (b-1)) = 1\). So, \(gcd(33, 20) = 1\).
- \(A\) computes RSA, \(n = a \cdot b, n = 3 \cdot 11 = 33\).
- Now Carmichael’s function, \(\lambda = lcm (a - 1, b - 1)\)
- \(\lambda = lcm (2, 20) = 10\)
- \(\lambda = (3 - 1)(11 - 1) / gcd (3 - 1, 11 - 1) = 20 / gcd(2, 20) = 10\)
- \(\lambda = 10\)
- \(Select\ g,\ randomly\ from\ G\ (G\ is\ a\ cyclic\ group\ of\ identities)\)
- \(gcd (g, \lambda) \mod n^2) / n, n = 1\)
- \(if\ g = 2,\ so\ gcd\ mod\ n^2 = 2^10 mod (33^2 - 1) = 20 mod 1088 = 20\)
- \(gcd (g, \lambda) \mod n^2) / (n, n = gcd (20/33 , 33) = gcd (0.606, 33) = 1\)
- \((Around\ 1,\ here\ we\ overlook\ fractional\ values)\)
- So, \(gcd (0.606, 33) = 1\)
- \(Calculate\ modular\ multiplicative\ inverse, \mu = ((g^4 \mod n^2) )^{-1} \mod n\)
- \(\mu = ((g^4 \mod n^2) )^{-1} \mod n\)
- \((\mu g^2 \mod n^2) )^{-1} = (2^10 \mod (33^2 - 1) = (1024\ mod 1089)^{-1} = 67\)
- \(\mu = ((g^4 \mod n^2) )^{-1} \mod n = 67\ mod 33 = 1\)
- \(The\ public\ (encryption)\ key\ is\ (n, g) = (33, 2)\).
- \(The\ private\ (decryption)\ key\ is\ \((\lambda, \mu) = (10, 1)\).\)

Step 1. Key Updating

- \(A\) computes \( z = g^{k_1}\)
- Random number from \(B’s\ id.\)
- \(z = 2^4 = 16\)
- \(G\ is\ a\ cyclic\ group\ of\ \(B’s\ identities\ so\ here\ we\ contain\ its\ value\ equal\ to\ last\ value\ of\ id.\)
- \(G = 30\).
- \(The\ public\ (encryption)\ key\ is\ (G, n, z, g) = (30, 33, 16, 2)\).
- \(The\ private\ (decryption)\ key\ is\ \((k_1, \lambda, \mu) = (4, 10, 1)\).

Step 2. Encryption

- \(B\) chooses a random number \(k_2\) from \((A’s\ identities)\), then calculates \(c_2 = g^{k_2}\).
- If \(k_2 = 3\). So, \(c_2 = g^{k_2} = 2^3 = 8\).
- \(B\) calculates the shared secret \(s = z^{k_2} = 16^3 = 4096\).
- \(S = 4096\).
- \(B\) maps his secret message \(m\) onto an element \(m’\) of \(G\), if \(m’ = 2\).
- Then \(c_2 = m^2 \cdot s = 2^4 \cdot 4096 = 65536\).
c₂ = 8192.

- B sends the ciphertext (c₁, c₂) to A
  (c₁, c₂) = (g^{k₁}, m^* \cdot z^{k₂})
  (c₁, c₂) = (2^{1}, 2^{16} \cdot (2^{1} \cdot 2^{2}))
  (c₁, c₂) = (8, 8192) = (8, 8192)

**Step 3. Decryption**

- Decryption done by ciphertext (c₁, c₂)
- A calculates the shared secret s=c₁^{k₁} = 8^{1} = 4096.
- S = 4096.
- Computes m'={c}_{2:S^{-1}}
- 2 = c₂ (4096)^{-1}
  c₂ = 8192.

Now we prove value of m' equal to c₂S⁻¹

c₂S⁻¹ = m \cdot z^{k₂} \cdot (g^{k₁k₂})⁻¹ = m' \cdot g^{k₁k₂} \cdot g^{k₁k₂} = \frac{m}{\text{ }}

c₂S⁻¹ = 2 \cdot (16 \cdot (2^{3})) \cdot (2^{3}) = m'

c₂S⁻¹ = 2 \cdot (4096) (4096)⁻¹ = 2 \cdot (2^{1})(2^{-1}) = m'

c₂S⁻¹ = 2 \cdot (1) = 2 \cdot (1) = m'

c₂S⁻¹ = m' = 2.

For Homomorphic encryption we take multiple messages like (m₁, m₂) and calculate its value same as our proposed algorithm. The value of Homomorphic property for m₁ and m₂ in I KC is equal to value of Homomorphic property for m₁ and m₂ in IEC.

So,

\[ E(m₁) \cdot E(m₂) = E(x₁) \cdot E(x₂) = E(x₁ + x₂ \mod m²) \]

**IV. CONCLUSION**

Presently high adequacy and high insurance of information transmission turn out to be a great deal more fundamental for system or distributed computing. In this paper our focal point of consideration is on half breed innovation for encode the cloud information. In this strategy key era done by some particular characters (PAN number and Mail ID) of other client’s utilizing IKC calculation which encoded and decoded by IEC. Here we chipped away at Hybrid Homomorphic Encryption strategy (Identity based Encryption Cryptosystem and Identity based Key Cryptosystem) are generally utilized two calculations of lopsided encryption innovation. Gathering of IEC and IKC restored to half and half calculation, for key era and security here we proposed three calculations which are capable to secure cloud information for the reason that Hybrid Homomorphic Encryption permits direct scrambled correspondence in distributed computing.

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